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Name: _____

Class:

Due Date:

A.1 Kinematics

Understandings

- The motion of bodies through space and time can be described and analyzed in terms of position, velocity, and acceleration.
- The velocity is the rate of change of position and acceleration is the rate of change of velocity.
- The change in position is the displacement.
- The difference between distance and displacement.
- The difference between the instantaneous and average values of velocity, speed, and acceleration, and how to describe them.
- The equations of motion for solving problems with uniformly accelerated motion as given by

$$\circ s = \frac{u+v}{2}t$$

$$\circ v = u + at$$

$$\circ s = ut + \frac{1}{2}at^{2}$$

$$\circ v^{2} = u^{2} + 2as$$

- \circ $\,$ Motion with uniform and non-uniform acceleration.
- The behavior of projectiles in the absence of fluid resistance, and the application of the equations of motion resolved into vertical and horizontal components.
- The qualitative effect of fluid resistance on projectiles, including time of flight, trajectory, velocity, acceleration, range, and terminal speed.

Equations

 $s = \frac{u+v}{2}t$ v = u + at $s = ut + \frac{1}{2}at^{2}$ $v^{2} = u^{2} + 2as$

Interesting facts

- The record for the tallest person in the world is Robert Wadlow who measured 272 cm. He died at the age of 22.
- The record for the tallest building in the world is the Burj Khalifa in the United Arab Emirates which is almost 830 m tall.
- The record for the tallest mountain above sea level is Mount Everest which is located between China and Nepal. It is measured to be about 8,848 m above sea level.
- The record for the lowest depth below sea level is the Mariana Trench which is about 10,984 m below sea level. Surprisingly both life and pollution is found near the bottom of the Marina Trench.
- The fastest baseball pitch ever recorded is from Aroldis Chapman at which was about 169.1 km/h or 46.97 m/s.

Super Ultimate Graphing Challenge

http://theuniverseandmore.com/

The solutions can be found on the YouTube channel Go Physics Go:

https://www.youtube.com/@gophysicsgo/playlists

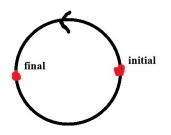
Part 1: Use your favorite sources to answer the following questions

- 1. C: What is the meaning of *zero dimensions*? *One dimension*? *Two dimensions*? *Three dimensions*? *Four dimensions*? If possible draw a figure for each.
- 2. C: Define *position*.
- 3. C: Define *distance*. Scalar or vector? Units? Example? Can *distance* be negative?
- 4. C: Define *displacement*. Scalar or vector? Units? Example? Can *displacement* be negative?
- 5. C: Define *speed*. Scalar or vector? Equation? Units? Example? Can *speed* be negative?
- 6. C: Define *velocity*. Scalar or vector? Equation? Units? Example? Can *velocity* be negative?
- 7. C: Define average speed. Scalar or vector? Equation? Units?
- 8. C: Define average velocity. Scalar or vector? Equation? Units?

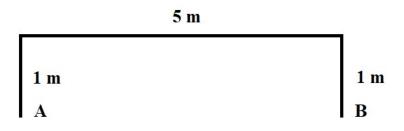
9. E: An object moves in a circle with a radius of 3.00 m. It takes the object 4.00 s to complete one revolution.



- a. What is the average speed and the average velocity of the object after it completes **one** cycle/revolution?
- b. What is the average speed and the average velocity of the object after it completes <u>one-half</u> cycle/revolution?



10.E: An object starts from rest at point A and then travels to point B by moving north 1.00 m, then east 5.00 m, and finally south 1.00 m in a total time of 14.0 s. What is the average speed and the average velocity of the object when it moves from point A to point B?



- 11.C: Define instantaneous speed. Example?
- 12.C: Define instantaneous velocity. Example?
- 13.C: Define *acceleration*. Equation? Units? Example? Can *acceleration* be negative?
- 14.C: What is the magnitude of the acceleration of free fall \vec{g} near the surface of the Earth? Which direction/way does it point? Is it positive or negative?

15.C: Define projectile motion.

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- 16.C: What does the slope of a *displacement vs. time* graph tell us? Equation? Units?
- 17.C: What does the slope of a velocity vs. time graph tell us? Equation? Units?
- 18.C: What does the slope of an *acceleration vs. time* graph tell us? Equation? Units?
- 19.C: What does the area under a *displacement vs. time* graph tell us? Units?
- 20.C: What does the area under a velocity vs. time graph tell us? Units?
- 21.C: What does the area under an acceleration vs. time graph tell us? Units?
- 22.C: How would you go about determining the acceleration due to gravity near the surface of the Earth? Which equation will you use? Which instruments do you need? What will you do?

23.C: Use a pencil and ruler! Define *terminal velocity*. What is the relationship between speed and the force of friction? Draw a *distance vs. time* graph, a *speed vs. time* graph, and an *acceleration vs. time* graph of an object being dropped from rest from a very high height above the surface of the Earth with both the force of friction and the force of gravity acting on it.

24.C: Use a pencil and ruler! Draw a *speed vs. time* graph of a skydiver first jumping out of an airplane, then reaching terminal velocity, then opening his parachute, then reaching a second terminal velocity, and finally hitting the ground.

25.C: A ball/projectile is thrown with an initial angle of 50.0° north of east. Draw its trajectory with no air friction and with air friction.

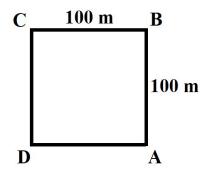
- 26.E: A ball is thrown vertically upwards with an initial velocity of 40.0 m/s in the absence of air friction. For this problem let the acceleration due to gravity be 10.0 m/s^2 down.
 - a. Complete the table below:

Time (s)	Acceleration $\left[\frac{m}{s^2}\right]$	Velocity $\left[\frac{m}{s}\right]$ $v_f = at + v_i$	Displacement [m] $y_{\rm f} = \frac{1}{2}at^2 + v_{\rm i}t + y_{\rm i}$	Total distance traveled [m]
0				
1				
2				
3				
4				
5				
6				
7				
8				

b. Use a pencil and ruler! Draw an *acceleration vs. time* graph, a *velocity vs. time* graph, a *speed vs. time* graph, a *displacement vs. time* graph, and a *distance vs. time* graph for the ball.

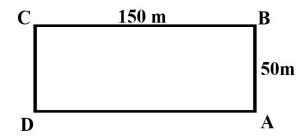
Part 2: Distance, Displacement, Speed, and Velocity

1. E: Wayde Van Niekerk from Russia runs 400. meters at a constant speed around a square track in a time of 43.03 s beginning at point A in a counterclockwise direction as shown below.



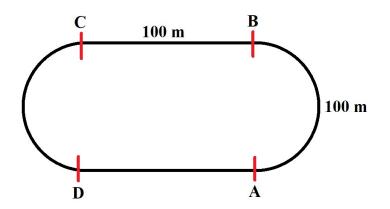
	Point B	Point C	Point D	Point A
Total Distance				
Total Displacement				
Average Speed				
Average Velocity				

2. E: Wayde Van Niekerk from Russia runs 400. meters at a constant speed around a rectangular track in a time of 43.03 s beginning at point A in a counterclockwise direction as shown below.



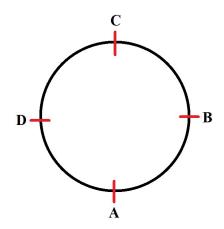
	Point B	Point C	Point D	Point A
Total Distance	50.0 m	200. m	250. m	400. m
Total Displacement				
Average Speed				
Average Velocity				

3. E: Wayde Van Niekerk from Russia runs 400. meters at a constant speed around an Olympic track in a time of 43.03 s beginning at point A in a counterclockwise direction as shown below. Each semicircle has an outer perimeter of 100. meters.



	Point B	Point C	Point D	Point A
Total Distance				
Total Displacement				
Average Speed				
Average Velocity				

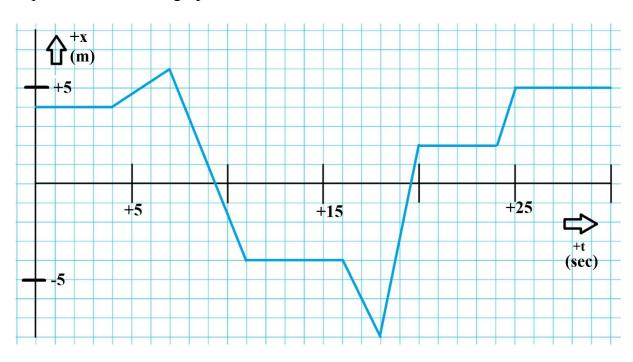
4. E: Wayde Van Niekerk from Russia runs 400. meters at a constant speed around a circular track in a time of 43.03 s beginning at point A in a counterclockwise direction as shown below.



	Point B	Point C	Point D	Point A
Total Distance				
Total Displacement				
Average Speed				
Average Velocity				

Part 3: Motion Graphs

1. E: An object can move to the left or right in one dimension. Positive displacement is towards the right and negative displacement is towards the left. Its *displacement vs. time* graph is shown below.



a. What does the slope of a *displacement vs. time* graph tell us?

b. Give all your solutions to two significant figures. Determine the *displacement* and *velocity* of the object at

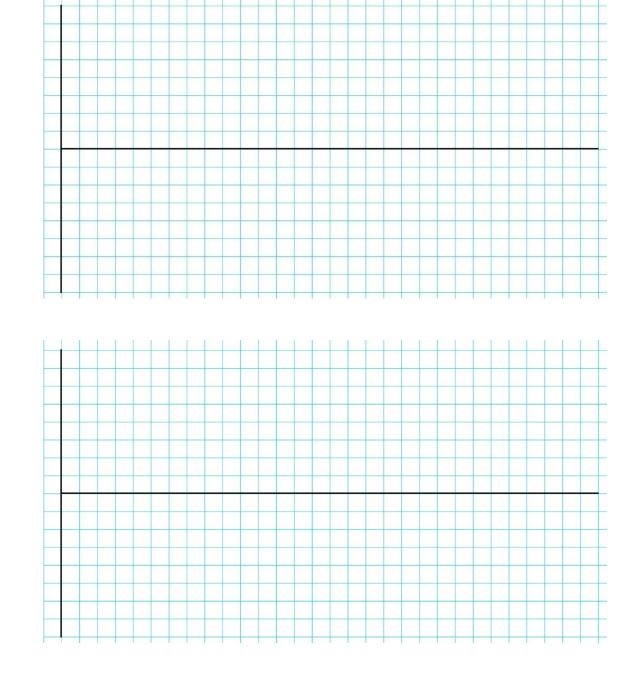
Time (s)	Displacement (m)	Velocity (m/s)
3.0		
5.0		
9.0		
13.0		
17.0		
19.0		
23.0		
24.5		
28		

c. What is the *total distance* the object travels from t = 0 s to t = 30 s?

d. What is the *displacement* of the object from t = 0 s to t = 30 s?

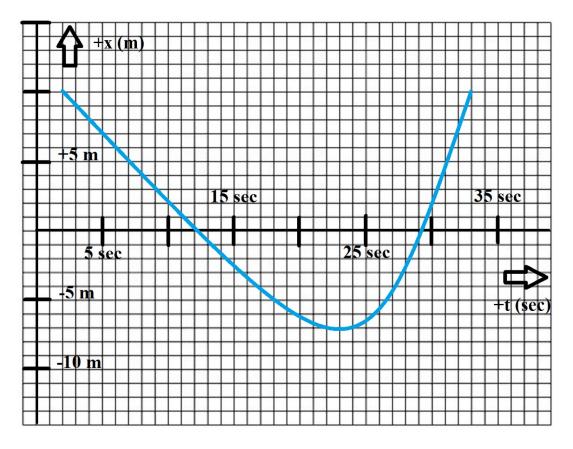
e. What does the slope of a *velocity vs. time* graph tell us?

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f. Use a pencil and ruler! Draw a *velocity vs. time* graph and an *acceleration vs. time* graph. Label your axes!

2. E: An object can move to the left or right in one dimension. Positive displacement is towards the right and negative displacement is towards the left. Its *displacement vs. time* graph is shown below.



a. Is the object moving to the left or the right? Is it speeding up or slowing down?

From $t = 2$ s to $t = 12$ s	
From $t = 12$ s to $t = 23$ s	
From $t = 23$ s to $t = 29$ s	
From $t = 29$ s to $t = 33$ s	

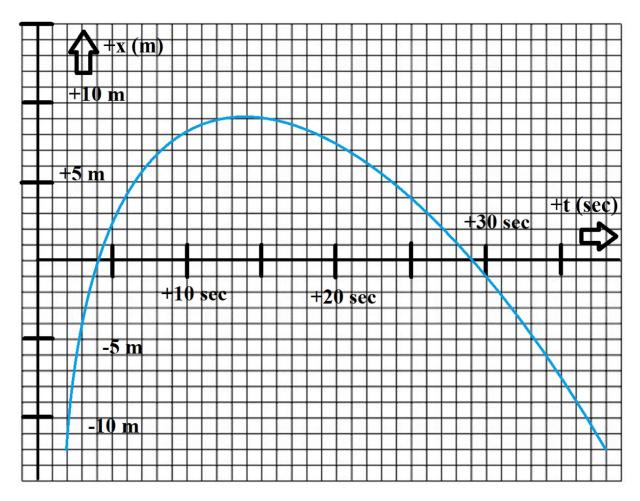
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b. Give all your solutions to two significant figures. Determine the *displacement* and *velocity* of the object at

Time (s)	Displacement (m)	Velocity (m/s)
12.		
23.		
29.		

- c. What is the *total distance* the object travels from t = 2 s to t = 33 s?
- d. What is the *displacement* of the object from t = 2 s to t = 33 s?

3. E: An object can move to the left or right in one dimension. Positive displacement is towards the right and negative displacement is towards the left. Its *displacement vs. time* graph is shown below.



a. Is the object moving to the left or the right? Is it speeding up or slowing down?

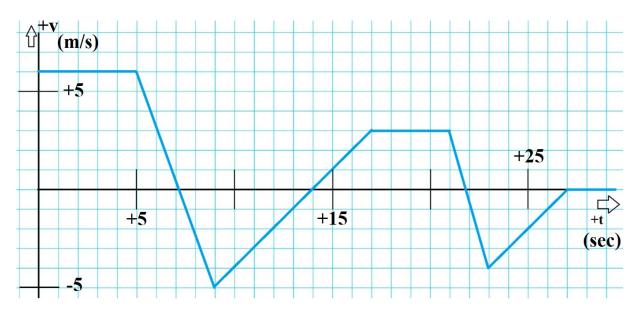
From $t = 2$ s to $t = 4$ s	
From $t = 4$ s to $t = 14$ s	
From $t = 14$ s to $t = 29$ s	
From $t = 29$ s to $t = 38$ s	

b. Give all your solutions to two significant figures. Determine the *displacement* and *velocity* of the object at

Time (s)	Displacement (m)	Velocity (m/s)
4.0		
14.		
29.		

- c. What is the *total distance* the object travels from t = 2 s to t = 38 s?
- d. What is the *displacement* of the object from t = 2 s to t = 38 s?

4. E: An object can move to the left or right in one dimension. Positive displacement is towards the right and negative displacement is towards the left. Its *velocity vs. time* graph is shown below.

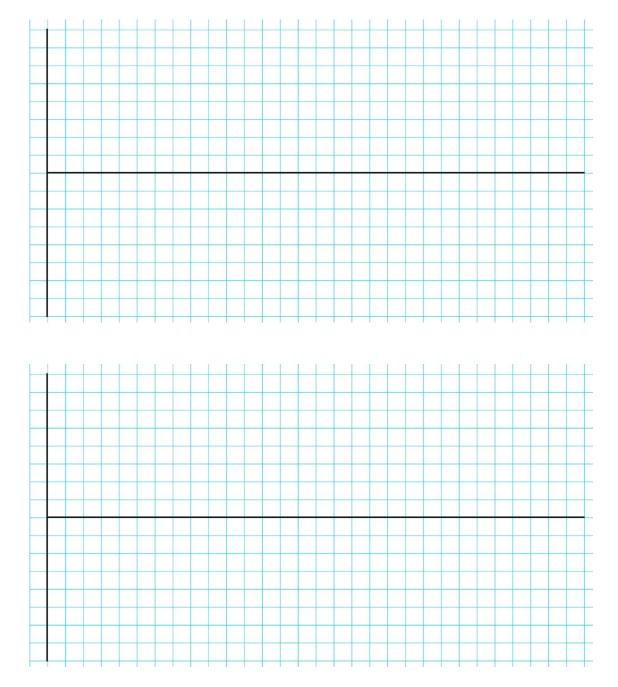


- a. What does the slope of a velocity vs. time graph tell us?
- b. Give all your solutions to two significant figures. Find the *velocity* and the *acceleration* of the object at

Time (s)	Velocity (m/s)	Acceleration (m/s^2)
3.0		
7.0		
8.0		
10.		
14.		
18.		
22.		
29.		

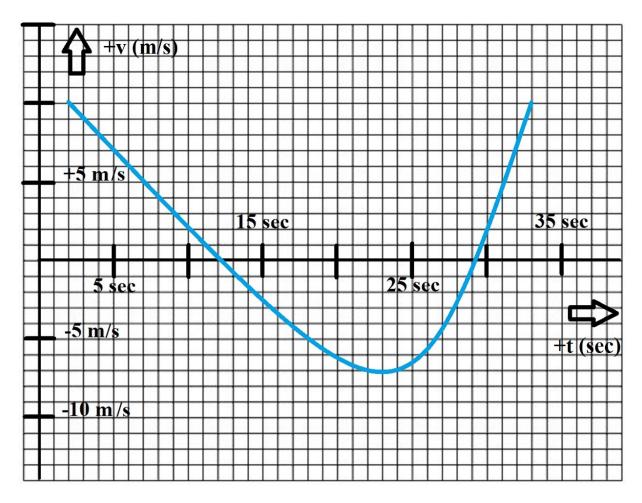
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- c. What does the area under a *velocity vs. time* graph tell us?
- d. Find the *displacement* of the object from
 - i. t = 0 s to t = 5 s
 - ii. t = 5 s to t = 9 s
- iii. t = 9 s to t = 17 s
- iv. t = 17 s to t = 27 s
- e. Determine the *total distance* the object travels from t = 0 s to t = 29 s.
- f. Determine the *displacement* of the object from t = 0 s to t = 29 s.



g. Use a pencil and ruler! Draw an *acceleration vs. time* graph and a *displacement vs. time* graph. Label your axes!

5. E: An object can move to the left or right in one dimension. Positive displacement is towards the right and negative displacement is towards the left. Its *velocity vs. time* graph is shown below.



a. Is the object moving to the left or the right? Is its acceleration increasing, decreasing, or constant?

From $t = 2$ s to $t = 12$ s	
From $t = 12$ s to $t = 23$ s	
From $t = 23$ s to $t = 29$ s	
From $t = 29$ s to $t = 33$ s	

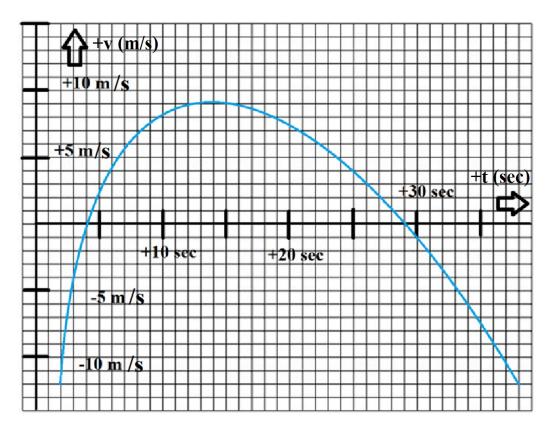
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b. Give all your solutions to two significant figures. Determine the *velocity* and *acceleration* of the object at

Time (s)	Velocity (m/s)	Acceleration (m/s^2)
12		
23		
29		

- c. Determine the *total distance* the object travels from t = 2 s to t = 33 s.
- d. Determine the *displacement* of the object from t = 2 s to t = 33 s.

6. E: An object can move to the left or right in one dimension. Positive displacement is towards the right and negative displacement is towards the left. Its *velocity vs. time* graph is shown below.



a. Is the object moving to the left or the right? Is its acceleration increasing, decreasing, or constant?

From $t = 2$ s to $t = 4$ s	
From $t = 4$ s to $t = 14$ s	
From $t = 14$ s to $t = 29$ s	
From $t = 29$ s to $t = 38$ s	

b. Give all your solutions to two significant figures. Determine the *velocity* and *acceleration* of the object during the following times:

Time [s]	Velocity [m/s]	Acceleration [m/s ²]
4		
14		
29		

- c. Determine the *total distance* the object travels from t = 2 s to t = 38 s.
- d. Determine the *displacement* of the object from t = 2 s to t = 38 s.

Part 4: Motion equations

There is no air friction for all the problems. The magnitude of the acceleration from gravity is 9.81 m/s^2 .

- 1. E: A car starts from rest and speeds up to 35.0 m/s in 12.0 s.
 - a. What is the average acceleration of the car during these 12.0 s?
 - b. What is the total distance traveled by the car during these 12.0 s?

The car then travels at a constant speed of 35.0 m/s for 900. m.

c. How long was the car travelling at this constant speed?

The car finally slows down from 35.0 m/s to 15.0 m/s in 4.00 s.

- d. What is the average acceleration (or deceleration) of the car during these 4.00 s?
- e. What is the total distance the car travels during these 4.00 s?
- f. What is the total distance the car travels since it started from rest?
- g. What is the total time taken for the car to travel since it started from rest until it reaches a speed of 15.0 m/s?

h. Use a pencil and ruler! Draw a *displacement vs. time* graph, a *velocity vs. time* graph, and an *acceleration vs. time* graph for the car.

- 2. E: A car starts from rest and accelerates at a constant rate of 4.00 m/s² for 8.00 s.
 - a. What is the speed of the car after 8.00 s?
 - b. How much distance did the car travel during these 8.00 s?

The car then moves at a constant speed for 12.0 s.

c. How much distance did the car travel during these 12.0 s?

The car then slows to a stop at a rate of 3.00 m/s^2 .

- d. How much time did it take for the car to decelerate and stop?
- e. How much distance did the car travel when it decelerates?

- f. What is the total time taken for the car to travel?
- g. What is the total distance taken for the car to travel?
- h. Use a pencil and ruler! Draw a *displacement vs. time* graph, a *velocity vs. time* graph, and an *acceleration vs. time* graph for the car.

- 3. E: Enoch throws a ball vertically upwards with an initial speed of 47.0 m/s at an elevation of 8,848 m above the surface of the Earth.
 - a. What will be the acceleration of the ball (number and direction) at the moment after it is thrown upwards?
 - b. What will be the acceleration of the ball (number and direction) when it reaches its maximum height?
 - c. What will be the velocity of the ball when it reaches its maximum height?
 - d. How long will it take for the ball to reach its maximum height?

- e. How many meters above the surface of the Earth will the ball be when it reaches its maximum height?
- f. What will be the acceleration of the ball (number and direction) just before it strikes the surface of the Earth?
- g. What will be the velocity of the ball when it is 8,950 m above the surface of the Earth?
- h. How long will it take for the ball to be 8,950 m above the surface of the Earth?
- i. What will be the velocity of the ball just before it strikes the ground?
- j. What is the total distance the ball travels during the first 4.50 s?
- k. What is the total distance the ball travels?
- 1. How long will it take for the ball to be 300. m above the surface of the Earth?

m. Use a pencil and ruler! Draw a *displacement vs. time* graph, a *velocity vs. time* graph, and an *acceleration vs. time* graph for the ball.

- 4. E: Noah drops a ball from rest at an elevation 830. m above the surface of the Earth.
 - a. What will be the acceleration of the ball (number and direction) at the moment it is dropped?
 - b. What will be the acceleration of the ball (number and direction) when it is 415. m above the surface of the Earth?
 - c. What will be the acceleration of the ball (number and direction) just before it strikes the surface of the Earth?
 - d. How long will it take for the ball to be 415 m above the surface of the Earth?
 - e. What will be the velocity of the ball 415 m above the surface of the Earth?
 - f. What will be the velocity of the ball just before it strikes the ground?

- g. What is the total distance the ball travels during the first 8.00 s?
- h. How long will it take for the ball to be 300. m above the surface of the Earth?
- i. What is the average speed of the ball?
- j. Use a pencil and ruler! Draw a *displacement vs. time* graph, a *velocity vs. time* graph, and an *acceleration vs. time* graph for the ball.

- 5. E: Eber throws a ball vertically downwards with an initial speed of 22.0 m/s from a height of 8,848 m above the surface of the Earth.
 - a. What will be the acceleration of the ball (number and direction) at the moment after it is thrown downwards?
 - b. What will be the acceleration of the ball (number and direction) just before it strikes the surface of the Earth?

- c. What will be the velocity of the ball just before it strikes the surface of the Earth?
- d. How long will it take for the ball to reach the surface of the Earth?
- e. What will be the velocity of the ball when it is 4,000 m above the surface of the Earth?
- f. How long will it take for the ball to reach 4,000. m above the surface of the Earth?
- g. What is the total distance the ball travels after 12.5 s?
- h. Use a pencil and ruler! Draw a *displacement vs. time* graph, a *velocity vs. time* graph, and an *acceleration vs. time* graph for the ball.

- 6. E: You are standing on the top of a building 135 m tall. You throw a ball upward with a velocity of 22.0 m/s. At the exact same moment a friend throws a second ball upward from the ground with a velocity of 46.0 m/s. These two balls then collide at some later time.
 - a. How long after these two balls are released will they collide?

- b. Where will these two balls be when they collide?
- c. What will be the velocity of each ball just as they collide?

- d. What will be the relative velocity between these two balls at the moment they collide?
- 7. E: From the top of a building 85.0 m tall a ball is dropped. At the same time another ball is thrown upward from the ground with a speed of 46.0 m/s.
 - a. How long after the balls are released will they hit?

- b. How long above the ground will these two balls hit?
- 8. E: You are on the top of a building 44.2 m tall. The adjacent building is 98.1 m tall. You throw the ball upward so that the ball lands on the roof of the adjacent building 4.15 s after the ball is thrown. What will be the speed of the ball when it lands on the roof?

- 9. E: You are rushing to the train station to catch your morning commute. The train leaves the train station from rest with an acceleration of 0.600 $\frac{\text{m}}{\text{s}^2}$. You arrive at the station exactly 4.00 s after the train leaves and you immediately start running after the train with a constant velocity of 8.50 m/s.
 - a. How long after the train leaves the station do you catch up with the train?

b. How far from the train station do you catch up with the train?

c. With what minimum speed would you have to run in order to catch up with the train?

- 10.E: A marble is rolling along a horizontal tabletop, which is 94.0 cm above the floor, when the marble reaches the edge of the table and then falls to the floor. How long will it take for the marble to strike the floor?
- 11.E: A rifle bullet, which has a mass of 57.0 g, is fired horizontally from a rifle which is held 94.0 cm above the floor, with a velocity of 385 m/s. How long will it take for the bullet to strike the floor?
- 12.E: A marble is fired horizontally from a launching device attached to the edge of a tabletop which is 94.0 cm above the floor. The marble then strikes the floor 2.35 m from the edge of the table.
 - a. How long will it take for the marble to reach the floor?
 - b. What is the initial velocity of the marble as it leaves the launching device?
 - c. What will be the horizontal velocity of the marble as it reaches the floor?

- d. What will be the vertical velocity of the marble as it reaches the floor?
- e. What will be the direction and magnitude of the velocity of the marble as it reaches the floor?
- 13.E: Salah throws a ball with an initial speed of 47.0 m/s at an angle of 30.0° north of east 830. meters above the surface of the Earth.
 - a. Complete the table:

$$\begin{array}{ll} x_{i} = & & y_{i} = \\ v_{i,x} = & & v_{i,y} = \\ a_{x} = & & a_{y} = \end{array}$$

- b. What will be the horizontal velocity and horizontal acceleration of the ball (number and direction) when it reaches its maximum height?
- c. What will be the vertical velocity and vertical acceleration of the ball (number and direction) when it reaches its maximum height?
- d. How long will the ball be in the air for?

- e. What will be the range (horizontal distance) of the ball?
- f. What will be the maximum height of the ball from the surface of the Earth after it is thrown?
- g. How long will it take for the ball to reach its maximum height after it is thrown?
- h. How long does it take for the ball to reach 400. m above the surface of the Earth after it is thrown?
- i. How high above the surface of the Earth will the ball be 8.00 s after it is thrown?
- j. How far horizontally does the ball travel during the first 8.00 s after it is thrown?
- k. What will be the velocity of the ball (number and direction) 8.00 s after it is thrown?

1. What will be the displacement of the ball (number and direction) 8.00 s after it is thrown?

m. Use a pencil and ruler! Draw an *acceleration vs. time* graph, a *velocity vs. time* graph, a *speed vs. time* graph, a *displacement vs. time* graph, and a *distance vs. time* graph for the ball for both the horizontal direction and the vertical direction.

- 14.E: A projectile, which has a mass of 5.50 kg, is fired from the ground with an initial velocity of 169. m/s at an angle of 23.0° above the horizontal.
 - a. Complete the following table:

$$x_i =$$
 $y_i =$ $v_{i,x} =$ $v_{i,y} =$ $a_x =$ $a_y =$

- b. What will be the velocity of this projectile at the highest point of its projectile?
- c. What will be the total flight time of this projectile?
- d. What will be the height of this projectile at the highest point of its trajectory?
- e. What will be the range of this projectile?
- f. What will be the vertical velocity of this projectile 3.50 s after it has been fired?
- g. What will be the horizontal velocity of this projectile 3.50 s after it has been launched?

h. What will be the direction and magnitude of the projectiles velocity 3.50 s after it has been fired?

- i. What will be the height of this projectile 3.50 s after it has been fired?
- j. How far downrange will the projectile be 3.50 s after it has been fired?
- k. What will be the final displacement of the projectile 3.50 s after the projectile has been fired?

15.E: A Spanish Galleon enters a harbor defended by cannon placed on top of a castle wall which is 135 m above the water level. The cannon have a known muzzle velocity of 323 m/s and are aimed 28.0° above the horizontal. How far from the base of the castle wall will the Galleon be within the range of the cannon?

- 16.E: A motorcycle is moving with a velocity of 36.0 m/s when it encounters a ramp which is 22.0 m long and meets the horizontal at an angle of 13.0°. The motorcycle goes up the incline without losing speed and flies off the end of the incline.
 - a. How long after the motorcycle leaves the end of the ramp will the motorcycle land on the ground?

- b. How far from the end of the ramp will the motorcycle land on the ground?
- c. How high above the ground will the motorcycle be at its highest point?
- 17.E: Abraham throws a ball horizontally eastward with an initial speed of 22.0 m/s from 830. m above the surface of the Earth.
- a. Complete the table:

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$x_{i} =$	$y_i =$
$v_{i,x} =$	$v_{i,y} =$
$a_{\rm x} =$	$a_y =$

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b. How long will the ball be in the air for after it is thrown?

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- c. What will be the range of the ball?
- d. How long does it take for the ball to reach 400. m above the surface of the Earth after it is thrown?
- e. How high above the surface of the Earth will the ball be 8.00 s after it is thrown?
- f. How far horizontally does the ball travel during the first 8.00 s after it is thrown?

g. What will be the velocity of the ball (number and direction) 8.00 s after it is thrown?

h. What will be the displacement of the ball (number and direction) 8.00 s after it is thrown?

- 18.E: Lot throws a ball at an initial speed of 12.0 m/s at an angle of 30.0° south of east from 830. m above the surface of the Earth.
 - a. Complete the table:

$$\begin{array}{ll} x_{\mathrm{i}} = & & y_{\mathrm{i}} = \\ v_{\mathrm{i},\mathrm{x}} = & & v_{\mathrm{i},\mathrm{y}} = \\ a_{\mathrm{x}} = & & a_{\mathrm{y}} = \end{array}$$

- b. How long will the ball be in the air for?
- c. What will be the range of the ball?
- d. How long after the ball is thrown does it take to reach 400. m above the surface of the Earth?
- e. How high above the surface of the Earth will the ball be 4.00 s after it is thrown?
- f. How far horizontally does the ball travel during the first 4.00 s after it is thrown?

g. What will be the velocity of the ball (number and direction) 4.00 s after it is thrown?

h. What will be the displacement of the ball (number and direction) 4.00 s after it is thrown?

19.E: A 25.0 kg ball is thrown from the edge of a very tall building with an initial speed of 20.0 m/s at an angle of 60.0° north of east. There is an infinitely tall vertical wall 120. m from the building.

a. Draw a figure.

b. Complete the table:	
$x_{i} =$	$y_i =$
$v_{i,x} =$	$v_{i,y} =$
$a_{\rm x} =$	$a_{y} =$

- c. How much time does it take for the ball to hit the wall?
- d. At which height above or below the original position where the ball is thrown will the ball hit the wall?

e. What will be the velocity of the ball (number and direction) when it hits the wall?

f. What will be the displacement of the ball (number and direction) when it hits the wall?