Name: $\qquad$

Class: $\qquad$

Due Date: $\qquad$

## A. 5 Galilean and Special Relativity

## Additional HL Understandings

- Reference frames.
- Newton's laws of motion are the same in all inertial reference frames and this is known as Galilean relativity.
- In Galilean relativity the position $x^{\prime}$ and time $t^{\prime}$ of an event are given by $x^{\prime}=x-v t$ and $t^{\prime}=t$.
- Galilean transformation equations lead to the velocity addition equation as given by $u^{\prime}=u-v$.
- Two postulates of special relativity.
- The postulates of special relativity lead to the Lorentz transformation equations for the coordinates of an event in two inertial reference frames as given by $x^{\prime}=\gamma(x-v t)$
$t^{\prime}=\gamma\left(t-\frac{v x}{c^{2}}\right)$
where $\gamma=\frac{1}{\sqrt{1-\frac{v^{2}}{c^{2}}}}$.
- Lorentz transformation equations lead to the relativistic velocity addition equation as given by $u^{\prime}=\frac{u-v}{1-\frac{u v}{c^{2}}}$.
- The space-time interval $\Delta s$ between two events is an invariant quantity as given by $(\Delta s)^{2}=(c \Delta t)^{2}-\Delta x^{2}$.
- Proper time interval and proper length.
- Time dilation as given by $\Delta t=\gamma \Delta t_{0}$.
- Length contraction as given by $L=\frac{L_{0}}{\gamma}$.
- The relativity of simultaneity.
- Space-time diagrams.
- The angle between the world line of a moving particle and the time axis on a space-time diagram is related to the particle's speed as given by $\tan \theta=\frac{v}{c}$.
- Muon decay experiments provide experimental evidence for time dilation and length contraction.


## Additional HL Equations

$x^{\prime}=x-v t$
$t^{\prime}=t$
$u^{\prime}=u-v$
$x^{\prime}=\gamma(x-v t)$ where $\gamma=\frac{1}{\sqrt{1-\frac{v^{2}}{c^{2}}}}$
$t^{\prime}=\gamma\left(t-\frac{v x}{c^{2}}\right)$
$u^{\prime}=\frac{u-v}{1-\frac{u v}{c^{2}}}$
$(\Delta s)^{2}=(c \Delta t)^{2}-\Delta x^{2}$
$\Delta t=\gamma \Delta t_{0}$
$L=\frac{L_{0}}{\gamma}$
$\tan \theta=\frac{v}{c}$

# The solutions can be found on the YouTube channel Go Physics Go: 

https://www.youtube.com/@gophysicsgo/playlists

1. Define observer.
2. Define reference frame.
3. Define inertial reference frame.
4. Define event.
5. Define simultaneous events.
6. Define and state the equations for Galilean transformations.

## 7. Define Galilean relativity.

8. State the two postulates of relativity.
9. A train is traveling horizontally to the right with a speed of $18 \frac{\mathrm{~m}}{\mathrm{~s}}$. A man on the train is walking to the right with a speed of $+4 \frac{\mathrm{~m}}{\mathrm{~s}}$. Determine the velocity of the man by an observer at rest outside the train.
10.Usain Bolt and Florence Griffith-Joyner race each other. They both begin at the same time. Usain Bolt runs with a constant speed of $10.44 \frac{\mathrm{~m}}{\mathrm{~s}}$ while Florence Griffith-Joyner runs with a constant speed of $9.53 \frac{\mathrm{~m}}{\mathrm{~s}}$.
a. What is the distance between Usain Bolt and the starting line after two minutes?
b. According to Florence Griffith-Joyner, what is the distance to Usain Bolt after two minutes?
c. Determine the speed of Usain Bolt as observed by Florence Griffith-Joyner.
11.What is the conclusion of the Michelson-Morley experiment?
10. State the Lorentz transformation equations. Define each variable.
11. State and draw a Lorentz factor vs. speed graph.
12. An event occurs at position $x=4,000 \mathrm{~m}$ and time $t=6.0 \mathrm{~s}$. Where and when did the event occur according to a rocket traveling horizontally in the positive direction at a speed of $v=0.4 c$ ? The origins of both reference frames are zero when both clocks read zero.
13. A rocket moves to the right past an IB school with a speed of $0.6 c$. The IB school is located at the origin. Determine the time reading of the rocket if $x=300 \mathrm{~m}$. The origins of both reference frames are zero when both clocks read zero.
14. Describe time dilation and proper time interval.
17.Describe length contraction and proper length.
15. Describe the twin paradox.
19.A man at rest sees two objects traveling towards each other each with a speed of $0.5 c$. What is the speed of one object as seen by the other object? What would this value be using classical physics?
20.Romeo is behind Juliet and is running towards her with a speed of $0.6 c$ as seen by a man at rest. Juliet is running away from Romeo with a speed of $0.4 c$ as seen by the same man at rest. What is the speed of Romeo as observed by Juliet? What would this value be using classical physics?
16. A rocket is moving in a straight line with a constant speed $v$ in space. It sends out a pulse of light ahead of it. How fast does the pulse of light move relative to an observer at rest on Earth?
17. A rocket at rest on Earth is measured to have a length of 45.0 meters and a diameter of 5.60 meters. The rocket is then launched toward Alpha Centauri, which is 4.3 light years from the Earth, at $2.2 \times 10^{8} \frac{\mathrm{~m}}{\mathrm{~s}}$.
a. What will be the length of this rocket as measured by an observer on the Earth?
b. What will be the length of the rocket as measured by an astronaut on board the rocket?
c. What will be the diameter of the rocket as measured by an observer on the Earth?
d. What will be the distance to Alpha Centauri as measured by the astronaut on board the rocket?
18. The distance to the star Epsilon Indi, as measured from the Earth frame of reference, is $1.07 \times 10^{17} \mathrm{~m}$.
a. What is this distance in light years?
b. What will be the distance in light years to Epsilon Indi as measured by an observer on a rocket heading toward this star at $85 \%$ of the speed of light?
c. How long in years will it take for this rocket to reach Epsilon Indi according to an observer on the Earth?
19. A rocket is moving toward the star Sirius with a velocity of $2.955 \times 10^{8} \frac{\mathrm{~m}}{\mathrm{~s}}$. The distance to Sirius as measured from the rest frame on Earth is measured to be $8.14 \times 10^{16} \mathrm{~m}$.
a. What will be the velocity of this rocket as a decimal fraction of the speed of light?
b. What is the distance to Sirius in light years?
c. What will be the distance to Sirius as measured by an astronaut on board the rocket?
20. As measured from the Earth the distance to Tau Ceti is determined to be 11.8 light years. How fast in $\frac{\mathrm{m}}{\mathrm{s}}$ must a rocket be moving toward Tau Ceti so that the distance to Tau Ceti is reduced to 1.18 light years?
21. How fast must a rocket be moving in order for its length to be reduced to $1.0 \%$ of its rest length?
27.According to an observer on the Earth the time it should take to reach a certain star is determined to be 7.50 years. How long will it take to reach this star according to an observer on board a rocket moving toward this star with a velocity of $0.985 c$ ?
22. The distance to Barnard's star is measured to be 6.00 ly by an observer at rest on the Earth.
a. Assuming that a rocket is moving toward this star at 0.98 c , how long in years will it take for this rocket to reach Barnard's star according to an observer on the Earth?
b. How long in years will it take to reach this star according to an observer on board the rocket?
c. What will be the distance in light years to Barnard's star according to an observer on board the rocket?
d. Assuming that the astronaut was 21 years old when she left the Earth in 1988, in what year will the astronaut arrive at Barnard's star according to an observer on Earth?
e. How old will the astronaut be when she arrives at Barnard's star according to an observer on board the rocket?
f. Suppose that the astronaut has a normal heart rate of 65 beats per minute when measured while at rest on the Earth. What will be the astronaut's heart rate as monitored by an observer on board the rocket with the astronaut?
g. What will the astronaut's heart rate be while on the rocket moving toward Barnard's star as monitored by an observer on the Earth?
23. Two astronauts play a game of chess on a rocket moving with a velocity of 0.999 c away from the Earth. According to the astronauts the game takes 2.5 hours. How long does the game take according to an observer at rest on Earth?
30.A rocket is moving toward Epsilon Eridani, which is 11.3 ly away as measured by an observer at rest on the Earth, at 0.998 c. When the astronaut leaves the Earth in 1991 he has just had his $22^{\text {nd }}$ birthday and his young daughter has just turned 1.0 years old. The rocket travels to the star, remains 6.0 months and then returns to the Earth at the same speed.
a. In what year will the rocket return to the Earth?
b. How many years will the journey take according to the astronaut on board the rocket?
c. How old will the astronaut be when he returns to the Earth?
d. How old will his daughter be when he returns to the Earth?
24. Two twins are 22.0 years old when one of them sets out on a journey through space with a constant speed. The twin in the spaceship measures time with an accurate watch. When he returns to Earth, he claims to be 28.0 years old while the twin left on Earth is 40.0 years old. What was the speed of the spaceship?
32.A neutron outside the confines of the nucleus of an atom is unstable and has a life expectancy (half-life) of 6.0 minutes. Suppose that a fast moving alpha particle collides with a block of beryllium and knocks a neutron out of the nucleus with a speed of $8.15 \times 10^{7} \frac{\mathrm{~m}}{\mathrm{~s}}$. What will be the expected lifetime of this neutron as measured by and observer in the rest frame?
33.Describe the equation of the space-time interval $\Delta s$. Describe proper time interval and proper length in terms of the space-time interval $\Delta s$.
34.Describe the relativity of simultaneity.
35.Draw and label the axes of a space-time diagram.
25. Draw a space-time graph where two events occur at the same time and another space-time graph where two events which occur at the same location.
37.Define the world line. Draw a world line in a space-time graph of an object at rest, a second object moving with a velocity of $0.4 c$, and a third object moving with a velocity of $0.8 c$.
26. Describe the relationship between the angle between the world line of a moving particle and the time axis on a space-time diagram.
39.Add another reference frame to a space-time diagram. On the space time diagram label an event and describe how that event takes place at two different times in both reference frames.
40.Draw a diagram with two reference frames. Label four stationary events in an $\left(x^{\prime}, c t^{\prime}\right)$ graph. Draw a second diagram with two reference frames. Label four events which occur at the same time in an $\left(x^{\prime}, c t^{\prime}\right)$ graph.
27. Below is a space-time diagram with two reference frames and five events. Determine the order of events according to the $(x, c t)$ graph and the $\left(x^{\prime}, c t^{\prime}\right)$ graph.

28. Draw and describe a graph of $\Delta s^{2}=-1$.
29. Draw and describe a graph of $\Delta s^{2}=+1$.
30. Three observers $L, M$, and $R$ are separated a distance $A$ from each other on a parallel line. They all travel from rest to a speed of $0.4 c$ to the right and remain a distance $A$ from each other. The observer in the middle $M$ sends out a light pulse in all directions. The light gets reflected from observer $L$ and observer $R$ and returns to $M$. Does observer $M$ receive the light pulse from observer $L$ or observer $R$ first?
31. Describe muon decay.
